

## Bleep test for Superman

The standard bleep test would clearly not be a challenge for someone as fast as our hero, so let's modify it slightly:



### Standard Test:

- Increase speed by  $0.5\text{km/h}$  at each stage.
- Each stage lasts for about 60 seconds.

### Superman Test:

- Increase speed by 20% at each stage.
- Each stage lasts for just one 20 metre length.

A speed increase of 20% corresponds to a decrease in time taken to run the 20 metres of  $\frac{1}{1.2}$  or 17%. Since he only does 20m at each stage, the stages will go by faster and faster, and it is impossible for the test, however many stages there may be, to take longer than a minute.

- Starting at  $2\text{ms}^{-1}$ , or  $7.2\text{km/h}$ , around the same as a standard test, Superman would be running as fast as the fastest 100m sprinters by stage 10, having run 200m in total and having been running for just over 50 seconds.
- By 57 seconds in, having completed the 17<sup>th</sup> stage, he is running fast enough to trigger motorway speed cameras.
- At stage 24 (just a couple of seconds later), he is outpacing formula 1 cars.
- He breaks the sound barrier at stage 30, 59.7 seconds in, and by the end of the next stage rivals fighter jets in speed.
- He breaks the airspeed record of  $2193\text{mph}$  (held by the Lockheed SR-71 Blackbird) after 59.9 seconds at stage 35, and before he's gone 1000 metres he is faster than the space shuttle's re-entry speed of  $17,500\text{mph}$ .
- At stage 54 he is now faster than the fastest man-made object, the Helios 2 Solar Probe which made a near-orbit of the sun at a top speed of  $157,000\text{mph}$ .
- There's very little to compare his speed to between stage 54 and stage 100, but it should be noted that his speed doubles 12 times until finally, still (just) less than a minute since starting the test, he matches the speed of light.

$$\text{Distance: } 20\text{m} \quad \text{Speed: } 2\text{ms}^{-1} \quad \text{Time: } \frac{20}{2} = 10\text{s}$$

Time taken forms a geometric series, first term:  $a = 10$  common ratio:  $r = \frac{5}{6}$

$$S_{\infty} = \frac{a}{1-r} = \frac{10}{\left(1 - \frac{5}{6}\right)} = \frac{10}{\frac{1}{6}} = \mathbf{60 \text{ seconds}}$$