Graph Transformations Investigation with Google's graphical calculator

Google incorporates a sophisticated calculator into its search engine. If you type something into the search box that Google interprets as the equation of a curve it will show it before the main search results.

By separating equations with commas, up to four different curves can be shown simultaneously.

Note: symbols are designed for keyboards: $\frac{x^3}{4}$ + 2 sin x is written as: (x^3)/4+2*sin(x)



Use the Google graphing function to investigate the following transformations.

Describe the change you notice in the graph as geometric transformations (eg "stretch of scale factor a in the x direction" or "translation of a upwards")

Transformation to investigate	Description of transformation
y = f(x) transformed to $y = f(x) + a$	
Eg:	
$y = \sin(x) \rightarrow y = \sin(x) + 2$	
	T
y = f(x) transformed to $y = f(x + a)$	
Eg: $2\sqrt{2}$ $2\sqrt{2}$ $2\sqrt{2}$ $2\sqrt{2}$ $2\sqrt{2}$ 1	
$y = 3x^2 - 2x \rightarrow y = 3(x+5)^2 - 2(x+5)$	
y = f(x) transformed to $y = af(x)$	

y = f(x) transformed to $y = af(x)$	
Eg:	
$y = x^3 - 2x \rightarrow y = 6(x^3 - 2x)$	

y = f(x) transformed to $y = f(ax)$	
Eg: $y = \cos(x) \rightarrow y = \cos(2x)$	

Extension: consider the last two transformations with a = -1. What do you notice?