

Centre Number						Candidate Number				
Surname										
Other Names										
Candidate Signature										



General Certificate of Education
Advanced Level Examination
January 2011

Mathematics

MFP2

Unit Further Pure 2

Wednesday 19 January 2011 1.30 pm to 3.00 pm

For this paper you must have:

- the blue AQA booklet of formulae and statistical tables.
- You may use a graphics calculator.

Time allowed

- 1 hour 30 minutes

Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- Write the question part reference (eg (a), (b)(i) etc) in the left-hand margin.
- You must answer the questions in the spaces provided. Do not write outside the box around each page.
- Show all necessary working; otherwise marks for method may be lost.
- Do all rough work in this book. Cross through any work that you do not want to be marked.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 75.

Advice

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.

For Examiner's Use	
Examiner's Initials	
Question	Mark
1	
2	
3	
4	
5	
6	
7	
8	
TOTAL	



J A N 1 1 M F P 2 0 1

Answer **all** questions in the spaces provided.

1 (a) Sketch on an Argand diagram the locus of points satisfying the equation

$$|z - 4 + 3i| = 5 \quad (3 \text{ marks})$$

(b) (i) Indicate on your diagram the point P representing z_1 , where both

$$|z_1 - 4 + 3i| = 5 \quad \text{and} \quad \arg z_1 = 0 \quad (1 \text{ mark})$$

(ii) Find the value of $|z_1|$. (1 mark)

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(ii) Find the value of $|z_1|$. (1 mark)

[illegible]

QUESTION
PART
REFERENCE

Turn over ►



2 (a) Given that

$$u_r = \frac{1}{6}r(r+1)(4r+11)$$

show that

$$u_r - u_{r-1} = r(2r+3) \quad (3 \text{ marks})$$

(b) Hence find the sum of the first hundred terms of the series

$$1 \times 5 + 2 \times 7 + 3 \times 9 + \dots + r(2r+3) + \dots \quad (3 \text{ marks})$$

QUESTION
PART
REFERENCE



QUESTION
PART
REFERENCE

Turn over ►



0 5

3 (a) Show that $(1 + i)^3 = 2i - 2$. (2 marks)

(b) The cubic equation

$$z^3 - (5 + i)z^2 + (9 + 4i)z + k(1 + i) = 0$$

where k is a real constant, has roots α , β and γ .

It is given that $\alpha = 1 + i$.

(i) Find the value of k . (3 marks)

(ii) Show that $\beta + \gamma = 4$. (1 mark)

(iii) Find the values of β and γ . (5 marks)

QUESTION
PART
REFERENCE



QUESTION
PART
REFERENCE

Turn over ►



4 (a) Prove that the curve

$$y = 12 \cosh x - 8 \sinh x - x$$

has exactly one stationary point.

(7 marks)

(b) Given that the coordinates of this stationary point are (a, b) , show that $a + b = 9$.

(4 marks)

QUESTION
PART
REFERENCE



QUESTION
PART
REFERENCE

Turn over ►



5 (a) Given that $u = \sqrt{1 - x^2}$, find $\frac{du}{dx}$. (2 marks)

(b) Use integration by parts to show that

$$\int_0^{\frac{\sqrt{3}}{2}} \sin^{-1} x \, dx = a\sqrt{3}\pi + b$$

where a and b are rational numbers.

(6 marks)

QUESTION
PART
REFERENCE



[illegible]

6 (a) Given that

$$x = \ln(\sec t + \tan t) - \sin t$$

show that

$$\frac{dx}{dt} = \sin t \tan t \quad (4 \text{ marks})$$

(b) A curve is given parametrically by the equations

$$x = \ln(\sec t + \tan t) - \sin t, \quad y = \cos t$$

The length of the arc of the curve between the points where $t = 0$ and $t = \frac{\pi}{3}$ is denoted by s .

Show that $s = \ln p$, where p is an integer. (6 marks)

QUESTION
PART
REFERENCE



[illegible]

P38405/Jan11/MFP2



(4 marks)

[illegible]

[illegible]

P38405/Jan11/MFP2



(3 marks)

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END OF QUESTIONS



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ANSWER IN THE SPACES PROVIDED**

