

# Projectile Motion

When an object is thrown or fired so that it moves freely under gravity, it follows a **parabolic** (quadratic) path.

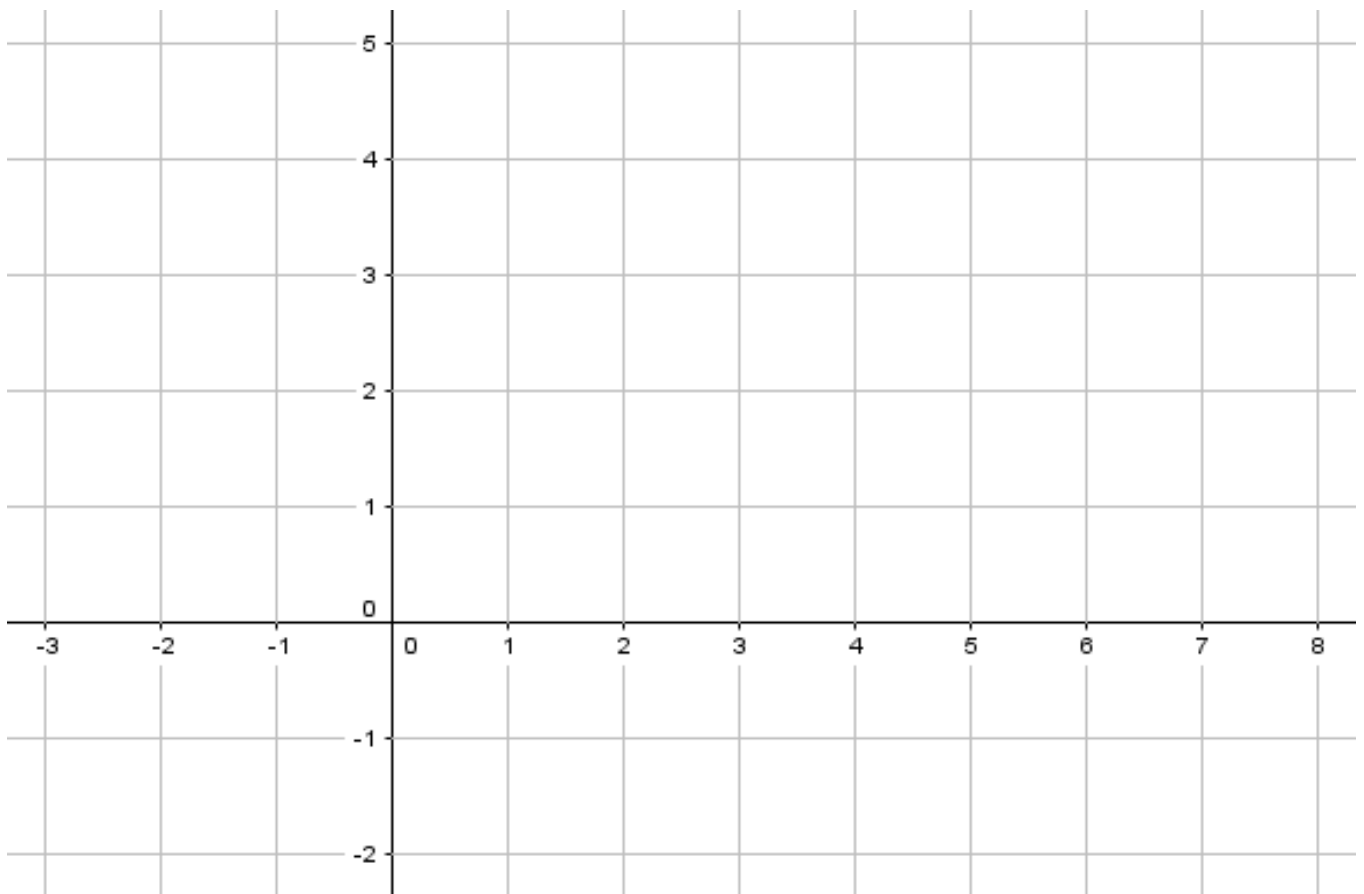
A ball is thrown at a speed of  $16\text{mph}$  at an angle of  $45^\circ$ . Its trajectory is described by:

$$y = 2 + x - 0.2x^2$$

where  $x$  is the horizontal distance travelled and  $y$  is the height (both in metres)

1. Use your calculator to complete the table of values and hence sketch the graph below.

$x$	0	1	2	3	4	5	6	7
$y$								



Your graph should be a smooth continuous curve which goes through each point you have plotted.

2. Use the graph to answer the following questions:

- What is the greatest height reached by the ball?
- What is the total (horizontal) range of the ball?
- During its flight, the ball passes over the top of a  $3\text{m}$  high fence. Where *could* it be?
- The graph crosses the  $y$ -axis at  $(0,2)$ . What does this tell you about the scenario?
- In reality, a ball thrown through the air may not follow a perfect parabola. Why?

## Projectile Motion SOLUTIONS

When an object is thrown or fired so that it moves freely under gravity, it follows a **parabolic** (quadratic) path.

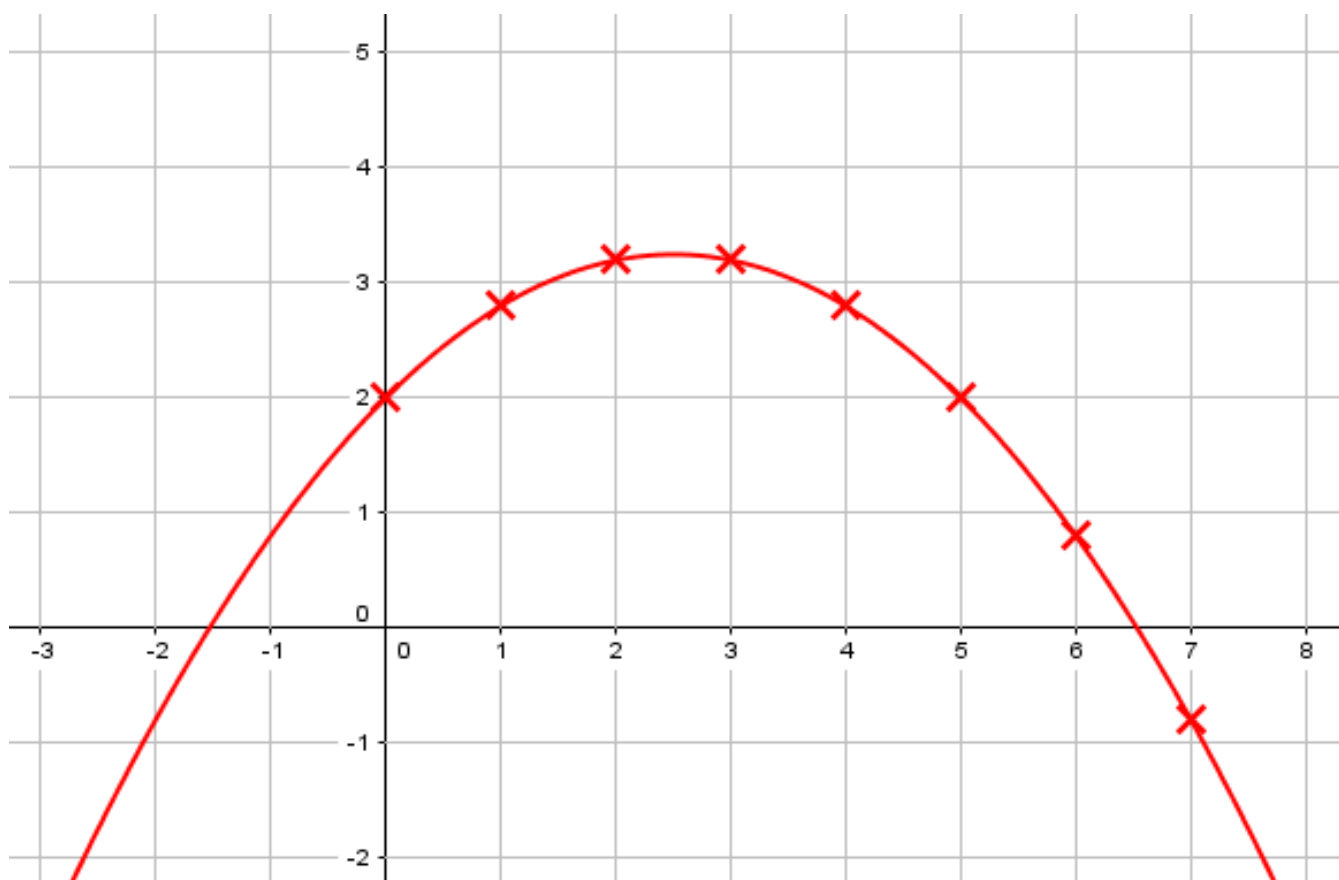
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$$y = 2 + x - 0.2x^2$$

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1. Use your calculator to complete the table of values and hence sketch the graph below.

$x$	0	1	2	3	4	5	6	7
$y$	2	2.8	3.2	3.2	2.8	2	0.8	-0.8



Your graph should be a smooth continuous curve which goes through each point you have plotted.

2. Use the graph to answer the following questions:

a) What is the greatest height reached by the ball?

**3.25m**

b) What is the total (horizontal) range of the ball?

**6.5m to 1 d. p.**

c) During its flight, the ball passes over the top of a 3m high fence. Where *could* it be?

**Between 1.4m and 3.6m from the thrower to 1 d. p.**

d) The graph crosses the y-axis at (0,2). What does this tell you about the scenario?

**The ball is thrown from an initial height of 2m**

e) In reality, a ball thrown through the air may not follow a perfect parabola. Why?

**Air resistance (especially if thrown very fast) affects it as well as gravity**