




# Vertical Circles *There are three main types of vertical circular motion, and each one must be treated differently.*

Type of Motion	Centripetal Force	High speeds	Lower speeds	Very low speeds	How to solve
<p><b><u>Inner Circles</u></b></p> <p>Eg:</p> <ul style="list-style-type: none"> <li>weight on a string</li> <li>car doing a loop-the-loop</li> </ul> 	<p>Provided by:</p> <p><b>Tension</b> in the string or <b>Normal reaction</b> of the track (acting radially) <b>combined with the radial component of weight.</b></p>	<p>The object describes <b>complete circles.</b></p>	<p>The object travels partway round the circle then <b>falls inwards</b> at the moment where <b>tension or normal reaction drops to zero.</b></p>	<p>If the object doesn't have enough energy to go beyond the halfway point it simply <b>oscillates</b> about the <b>lowest point</b> of the circle.</p>	<p><b>Energy:</b> to find the speed at a particular point. <b>Forces:</b> resolving radially and applying <math>F = ma</math> to find tension or normal reaction at a specific point. <b>This cannot be negative if the string is taut (or the object is in contact with the surface),</b> so if it reaches 0, the object is on the point of falling inwards.</p>
<p><b><u>Outer Circles</u></b></p> <p>Eg:</p> <ul style="list-style-type: none"> <li>object balanced on a sphere</li> <li>car driving over a bridge</li> </ul> 	<p>Provided by:</p> <p><b>Normal reaction</b> (acting <i>away from</i> the centre), <b>combined with the radial component of weight.</b></p>	<p>Once the normal reaction becomes zero, the object <b>falls outwards</b> from the circular path.</p>	<p>While there is still a normal reaction force acting away from the centre, the object will continue to travel in <b>circular motion.</b></p>	<p>While there is still a normal reaction force acting away from the centre, the object will continue to travel in <b>circular motion.</b></p>	<p><b>Energy:</b> to find the speed at a particular point. <b>Forces:</b> resolving radially and applying <math>F = ma</math> to find the normal reaction at a specific point. <b>This cannot be negative if the object is still in contact with the surface,</b> so the instant it reaches 0, the object is on the point of falling outwards.</p>
<p><b><u>Fixed Circles</u></b></p> <p>Eg:</p> <ul style="list-style-type: none"> <li>roller-coaster car on a track</li> <li>bead threaded on a wire</li> </ul> 	<p>Provided by:</p> <p><b>Normal reaction</b> (acting either <i>towards</i> or <i>away from</i> the centre), <b>combined with the radial component of weight.</b></p>	<p>The object describes <b>complete circles</b> and the normal reaction acts <b>towards the centre.</b></p>	<p>The object may still describe <b>complete circles</b>, but the normal reaction will be acting <b>away from the centre</b> for the part of the motion when the speed is very low.</p>	<p>The object <b>oscillates</b> about the lowest point if the <b>speed</b> drops to 0 before reaching the top. Normal reaction may point <b>towards or away from the centre.</b></p>	<p><b>Energy:</b> to find the speed at a particular point. <b>Forces:</b> resolving radially and applying <math>F = ma</math> to find the normal reaction at a specific point. <b>May be positive or negative,</b> as the normal reaction may point in or outwards. Since the object cannot leave the circular path, the key factor is the <b>speed of motion</b> at each point.</p>