

False Positive



Almost all medical tests have a small chance of a 'false positive' or a 'false negative'.

- **False positive:** The test says you **do** have the condition when you really **don't**.

(you're fine, but the test thinks you're sick)

- **False negative:** The test says you **don't** have the condition when you really **do**.

(you're sick, but the test thinks you're fine)

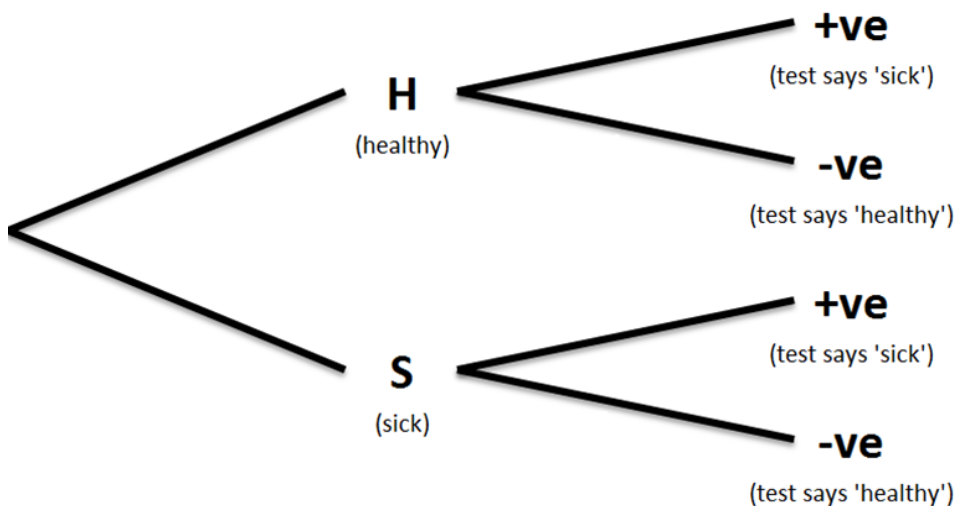
- The test for a particular disease has a false positive rate of 5%.

*This means that 5% of people who **don't** have the disease will be told that they **do**.*

- The test has a false negative rate of 1%.

*This means that 1% of people who **do** have the disease will be told that they **don't**.*

Assuming this particular disease affects 10% of people, complete the tree diagram below:



Use the tree diagram to calculate the probabilities for each of the four outcomes:

	Healthy	Sick
Tested Positive		<p><i>You're sick, and the test was correct</i></p>
Tested Negative	<p><i>You're fine, and the test was correct</i></p>	<p><i>You're sick, but the test thinks you're fine</i> FALSE NEGATIVE: You may not get the treatment you need.</p>

You're fine, but the test thinks you're sick
FALSE POSITIVE:
You may get treatment you don't need, or be worried for no reason.

If the test says I'm sick, what is the chance that I really am?

Hint: Imagine 1000 people take the test. Work out how many would test positive, and out of those people, how many are really sick?

False Positive SOLUTIONS



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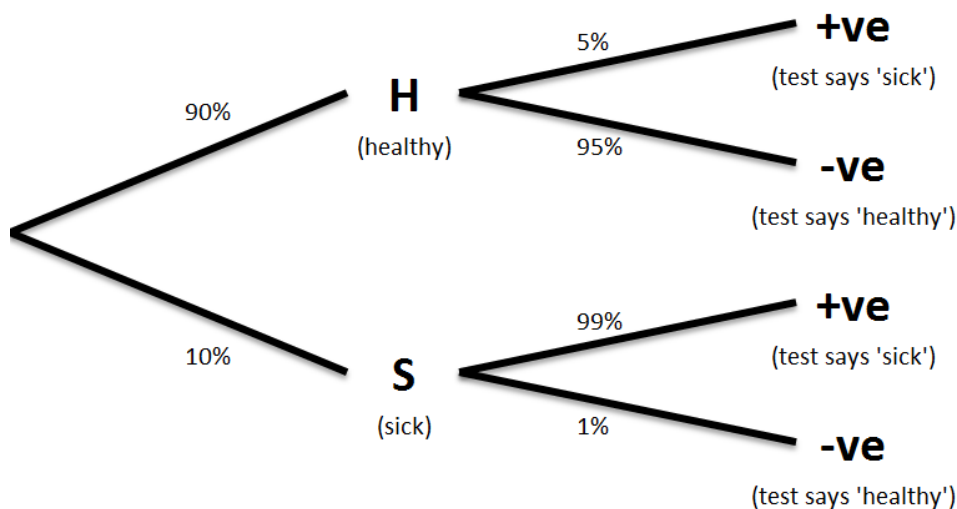
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Assuming this particular disease affects 10% of people, complete the tree diagram below:



Use the tree diagram to calculate the probabilities for each of the four outcomes:

$$0.9 \times 0.05 = \mathbf{0.045} \quad 0.9 \times 0.95 = \mathbf{0.855} \quad 0.1 \times 0.99 = \mathbf{9.9} \quad 0.1 \times 0.01 = \mathbf{0.001}$$

	Healthy	Sick
Tested Positive	4.5%	9.9%
Tested Negative	85.5%	0.1%

You're sick, and the test was correct (arrow to 9.9%)

You're sick, but the test thinks you're fine
FALSE NEGATIVE:
You may not get the treatment you need. (arrow to 0.1%)

You're fine, but the test thinks you're sick
FALSE POSITIVE:
You may get treatment you don't need, or be worried for no reason. (arrow to 4.5%)

You're fine, and the test was correct (arrow to 85.5%)

If the test says I'm sick, what is the chance that I really am?

For every 1000 people, $45 + 99 = 144$ of the population will test positive.

Of that 144, 99 are genuinely sick.

$$\frac{99}{144} = 0.6875 = \mathbf{68.75\% \text{ chance that you're really sick.}}$$