

## How to factorise any quadratic starting with $x^2$

Notice that  $(x + p)(x + q) = x^2 + px + qx + pq = x^2 + (p + q)x + pq$

This means that the numbers that will go in the brackets must:

- **Multiply** to make the **constant** term (number at the end)
- **Add** to make the  **$x$  coefficient** (number in front of  $x$ )

Eg:

$$x^2 + 9x + 20 = (x + \dots)(x + \dots)$$

I need two numbers which **multiply** to make **20** and **add** to make **9**:

$$4 \times 5 = 20 \quad \text{and} \quad 4 + 5 = 9$$

$$\text{So ... } x^2 + 9x + 20 = (x + 4)(x + 5)$$

### What about negatives?

The rules above still work, but it is made easier by thinking about the different possibilities and what it means about the numbers. You can tell what sign the two numbers need to be just by looking at the sign of their **product** and their **sum**:

Complete these statements:

If the **product** of  $p$  and  $q$  is **positive**, and the **sum** of  $p$  and  $q$  is **positive**, then ...

If the **product** of  $p$  and  $q$  is **positive**, and the **sum** of  $p$  and  $q$  is **negative**, then ...

If the **product** of  $p$  and  $q$  is **negative**, and the **sum** of  $p$  and  $q$  is **positive**, then ...

If the **product** of  $p$  and  $q$  is **negative**, and the **sum** of  $p$  and  $q$  is **negative**, then ...

Factorise the following quadratics:

$x^2 + 8x + 15$	$x^2 + 13x + 40$	$x^2 + 1000x + 999$
$x^2 - 6x + 8$	$x^2 - 6x - 16$	$x^2 + 12x - 45$
$x^2 - 17x - 60$	$6x^2 - 42x - 360$	$-x^3 - 15x^2 + 100x$

Hint: for the last two, remember that before you worry about double brackets, you can always use simple factoring techniques such as:  $6x + 12 = 6(x + 2)$  and  $-x^4 + x^2 = -x^2(x^2 - 1)$

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Complete these statements:

If the **product** of  $p$  and  $q$  is **positive**, and the **sum** of  $p$  and  $q$  is **positive**, then ...

***$p$  and  $q$  must both be positive***

If the **product** of  $p$  and  $q$  is **positive**, and the **sum** of  $p$  and  $q$  is **negative**, then ...

***$p$  and  $q$  must both be negative***

If the **product** of  $p$  and  $q$  is **negative**, and the **sum** of  $p$  and  $q$  is **positive**, then ...

***One will be positive, one negative (the larger will be positive)***

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Factorise the following quadratics:

$x^2 + 8x + 15$ $= (x + 3)(x + 5)$	$x^2 + 13x + 40$ $= (x + 5)(x + 8)$	$x^2 + 1000x + 999$ $= (x + 1)(x + 999)$
$x^2 - 6x + 8$ $= (x - 2)(x - 4)$	$x^2 - 6x - 16$ $= (x - 8)(x + 2)$	$x^2 + 12x - 45$ $= (x + 15)(x - 3)$
$x^2 - 17x - 60$ $= (x - 20)(x + 3)$	$6x^2 - 42x - 360$ $= 6(x^2 - 7x - 60)$ $= 6(x - 12)(x + 5)$	$-x^3 - 15x^2 + 100x$ $= -x(x^2 + 15x - 100)$ $= -x(x + 20)(x - 5)$

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